

Dilatação Térmica dos Líquidos – Lista 2:

Resolução

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1. B

2.

$$\gamma = 3 \cdot \alpha$$

$$\gamma = 3 \cdot 40 \cdot 10^{-6}$$

$$\gamma = 1,2 \cdot 10^{-4} \text{ } ^\circ\text{C}^{-1}$$

$$\Delta V_{\text{ap}} = V_0 \gamma_{\text{ap}} \Delta T$$

$$6 \cdot 10^{-2} \cdot 1 \cdot 10^{-7} = 1 \cdot 10^{-5} \cdot 1,2 \cdot 10^{-4} \cdot (T_s - 12)$$

$$T_s = 17^\circ\text{C}$$

3.

$$\Delta V_{\text{liq}} = \Delta V_{\text{frasco}}$$

$$V_0 \text{liq} \gamma_{\text{liq}} \Delta T = V_0 \text{frasco} \gamma_{\text{frasco}} \Delta T$$

$$0,8 \cdot V_0 \text{frasco} \gamma_{\text{liq}} = V_0 \text{frasco} \gamma_{\text{frasco}}$$

$$\gamma_{\text{frasco}} / \gamma_{\text{liq}} = 0,8$$

4.

$$\gamma_{\text{liq}} = \gamma_{\text{ap}} + \gamma_{\text{frasco}}$$

$$180 \cdot 10^{-6} = \gamma_{\text{ap}} + 9 \cdot 10^{-6}$$

$$\gamma_{\text{ap}} = 1,71 \cdot 10^{-4} \text{ } ^\circ\text{C}^{-1}$$

$$\Delta V_{\text{ap}} = V_0 \gamma_{\text{ap}} \Delta T$$

$$\Delta V_{\text{ap}} = 0,5 \cdot 1,71 \cdot 10^{-4} \cdot [90 - (-10)]$$

$$\Delta V_{\text{ap}} = 8,55 \cdot 10^{-3} \text{ cm}^3$$

$$S = S_0 [1 + \beta \Delta T]$$

$$S = 3 \cdot 10^{-4} \{1 + 6 \cdot 10^{-6} \cdot [90 - (-10)]\}$$

$$S = 3,0018 \cdot 10^{-4} \text{ cm}^2$$

(observe que, apesar de bem pouco, a área da secção transversal também dilata)

$$V = S \cdot h$$

$$8,55 \cdot 10^{-3} = 3,0018 \cdot 10^{-4} \cdot h$$

$$h \approx 28,48 \text{ cm}$$

5.

$$\Delta V_{\text{ap}} = V_0 \gamma_{\text{ap}} \Delta T$$

$$0,04 V_0 = V_0 \gamma_{\text{ap}} (80 - 0)$$

$$\gamma_{\text{ap}} = 5 \cdot 10^{-4} \text{ } ^\circ\text{C}^{-1}$$

$$\gamma_{\text{liq}} = \gamma_{\text{ap}} + \gamma_{\text{frasco}}$$

$$\gamma_{\text{liq}} = 5 \cdot 10^{-4} + 27 \cdot 10^{-6}$$

$$\gamma_{\text{liq}} = 5,27 \cdot 10^{-4} \text{ } ^\circ\text{C}^{-1}$$

6.

$$\gamma_{\text{liq}} = \gamma_{\text{ap}} + \gamma_{\text{frasco}}$$

$$10,7 \cdot 10^{-4} = \gamma_{\text{ap}} + 0,7 \cdot 10^{-4}$$

$$\gamma_{\text{ap}} = 1 \cdot 10^{-3} \text{ } ^\circ\text{C}^{-1}$$

$$\Delta V_{\text{ap}} = V_0 \gamma_{\text{ap}} \Delta T$$

$$\Delta V_{\text{ap}} = V_0 \cdot 1 \cdot 10^{-3} (35 - 15)$$

$$\Delta V_{\text{ap}} = 0,02 \cdot V_0$$

Transborda 2% do volume inicial de líquido.

7.

O frasco estará completamente cheio quando os volumes finais do frasco e do líquido forem iguais:

$$V_{\text{frasco}} = V_{\text{liq}}$$

$$V_0 \text{frasco} \cdot [1 + \gamma_{\text{frasco}} \Delta T] = V_0 \text{liq} \cdot [1 + \gamma_{\text{liq}} \Delta T]$$

$$V_0 \text{frasco} \cdot [1 + 5,1 \cdot 10^{-5} \cdot (T - 10)] = 0,95 \cdot V_0 \text{frasco} \cdot [1 + 5,8 \cdot 10^{-4} \cdot (T - 10)]$$

$$T = 110^\circ\text{C}$$

8.

a)

$$\Delta V_{\text{liq}} = V_0 \text{liq} \cdot \gamma_{\text{liq}} \cdot \Delta T$$

$$\Delta V_{\text{liq}} / V_0 \text{liq} = 9 \cdot 10^{-4} \cdot 40$$

$$\Delta V_{\text{liq}} / V_0 \text{liq} = 0,036$$

$$\Delta V_{\text{liq}} / V_0 \text{liq} = 3,6\%$$

b)

$$V_{\text{frasco}} = V_0 \text{frasco} \cdot [1 + \gamma_{\text{frasco}} \Delta T]$$

$$V_{\text{frasco}} = V_0 \text{frasco} \cdot [1 + 1 \cdot 10^{-5} \cdot 40]$$

$$V_{\text{frasco}} = V_0 \text{frasco} \cdot 1,0004$$

$$V_{\text{liq}} = V_0 \text{liq} \cdot [1 + \gamma_{\text{liq}} \Delta T]$$

$$V_{\text{liq}} = 0,97 \cdot V_0 \text{frasco} \cdot [1 + 9 \cdot 10^{-4} \cdot 40]$$

$$V_{\text{liq}} = V_0 \text{frasco} \cdot 1,00492$$

Como $V_{\text{liq}} > V_{\text{frasco}}$, o líquido transborda.

c)

$$\Delta V_{\text{liq}} = V_0 \text{liq} \cdot \gamma_{\text{liq}} \cdot \Delta T$$

$$\Delta V_{\text{liq}} = 40 \cdot 9 \cdot 10^{-4} \cdot 40$$

$$\Delta V_{\text{liq}} = 1,44 \text{ L}$$

$$\text{Economia} = 1,44 \text{ L} \cdot 2,50 \text{ reais/L} = \text{R}\$3,60.$$

9. C

10.

$$\gamma_{\text{liq}} = \gamma_{\text{ap}} + \gamma_{\text{frasco}}$$

$$X = \gamma_{\text{ap}} + Y$$

$$\gamma_{\text{ap}} = X - Y$$

$$\Delta V_{\text{ap}} = V_0 \cdot \gamma_{\text{ap}} \cdot \Delta T$$

$$V_H = V_B \cdot (X - Y) \cdot 1$$

$$V_H / V_B = X - Y$$